

SYSTEM AND METHOD FOR IMPROVING IMAGE QUALITY IN PROCESSED IMAGES

BACKGROUND OF THE INVENTION

5 **Field of the Invention**

The present disclosure relates to systems and methods for processing digital image signals. More particularly, the invention relates to a system and method that improves image quality by reducing the harshness of distortions in compressed digital image signals.

10

Discussion of the Related Art

A digital image signal generally contains information associated with a plurality of picture elements, *e.g.*, pixels. Digital images typically contain large amounts of information (*e.g.*, color and brightness information related to each of the plurality of pixels) needed to reproduce the image. As a result, data compression is often implemented to reduce the amount of memory that images require for processing and storage. Data compression is important not just for long term digital storage of an image but for permitting reasonable data transfer rates over network connected devices.

20 JPEG is a standardized image compression mechanism. JPEG stands for Joint Photographic Experts Group, the original name of the committee that wrote the standard. JPEG is designed for compressing either full-color or gray-scale digital images of "natural," real-world scenes. JPEG compression does not work very well on non-realistic images, such as cartoons or line drawings. JPEG compression does
25 not handle black-and-white (1-bit-per-pixel) images, nor does it handle motion picture compression. Related standards for compressing those types of images exist, and are called JBIG and MPEG respectively. Regular JPEG is "lossy," meaning that the image you get out of decompression is not identical to what you originally put in. The algorithm achieves much of its compression by exploiting known limitations of the

human eye, notably the fact that small color variations are not perceived as well as small variations in brightness.

The JPEG compression process is a multi-parameter compression process. By adjusting the parameters, you can trade off compressed image size against reconstructed image quality over a very wide range. In general, the baseline JPEG compression process performs the following steps:

1. Transform the image into a suitable color space. This is a no-op for grayscale images. For color images, RGB information is transformed into a luminance/chrominance color space (*e.g.*, YCbCr, YUV, *etc.*). The luminance component is grayscale and the other two axes are color information.
2. (Optional) Down sample each component by averaging together groups of pixels. The luminance component is left at full resolution, while the chroma components are often reduced 2:1 horizontally and either 2:1 or 1:1 (no change) vertically. In JPEG, these alternatives are usually called 2h2v and 2h1v sampling, but you may also see the terms "411" and "422" sampling. This step immediately reduces the data volume by one-half or one-third. In numerical terms it is highly lossy, but for most images it has almost no impact on perceived quality, because of the eye's poorer resolution for chroma info. Note that down sampling is not applicable to grayscale data; this is one reason color images are more compressible than grayscale.
3. Group the pixel values for each component into 8x8 blocks. Transform each 8x8 block through a discrete cosine transform (DCT). The DCT is a relative of the Fourier transform and likewise gives a frequency map, with 8x8 components. Thus you now have numbers representing the average value in each block and successively higher-frequency changes within the block. The motivation for doing this is that you can now throw away high-frequency information without affecting low-frequency information. (The DCT transform itself is reversible except for round off error.)
4. In each block, divide each of the 64 frequency components by a separate "quantization coefficient" and round the results to integers. This is the fundamental information-losing step. The larger the quantization coefficients, the more data is discarded. Note that even the minimum possible quantization coefficient, 1, loses some info, because the exact DCT outputs are typically not integers. Higher frequencies are always quantized less accurately (given larger coefficients) than lower, since they are less visible to the eye. Also,

the luminance data is typically quantized more accurately than the chroma data, by using separate 64-element quantization tables.

- 5 5. Encode the reduced coefficients using either Huffman or arithmetic coding.
6. Tack on appropriate headers, etc., and output the result. In normal "interchange" JPEG file, all of the compression parameters are included in the headers so that the decompressor can reverse the process. These parameters include the quantization tables and the Huffman coding tables.

(See generally pages 1-2 "Introduction to JPEG"
<http://www.faq.org/faqs/compression-faq/part2/section-6.html>)

A series of digital image signals may be concatenated (*i.e.*, strung together in series) to form a video or video sequence. Consider the case of a video sequence where nothing is moving in the scene. Each frame of the video should be exactly the same as the previous frame. In a digital system, it should be clear that a single frame and a repetition count could represent this video sequence.

Consider now, a man walking across the same scene. If information regarding the motion of the man can be extracted from the static background a great deal of storage space can be saved. This oversimplified case reveals two of the most difficult problems in motion compensation: 1) determining if an image is stationary; and 2) determining how and what portion of an image to extract for the portion of the image that moves.

These problems are addressed in the Moving Pictures Experts Group (MPEG) digital video and audio compression standard. In particular, the standard defines a compressed bit stream, which implicitly defines a decompressor. The most fundamental difference between MPEG and JPEG is MPEG's use of block-based motion compensated prediction (MCP), a general method which uses a temporal differential pulse code modulation (DPCM) scheme.

Usually, MCP and related block-based error coding techniques perform well when the image can be modeled locally as translational motion. However, when there is complex motion or new imagery, these error coding schemes may perform poorly, and the error signal may be harder to encode than the original signal. In such cases, it

is sometimes better to suppress the error-coding scheme and code the original signal itself. It may be determined on a block-by-block basis whether to use an error-coding scheme and code the error signal, or to simply code the original signal. This type of coding is often referred to as inter/intra processing, because the encoder switches
 5 between inter-frame and intra-frame processing.

Block-based MCP and inter/intra decision-making are the basic temporal processing elements for many conventional video compression standards. Generally, these block-based temporal processing schemes perform well over a wide range of image scenes, enable simpler implementation than other approaches, and interface
 10 reasonably well with any block DCT processing of the error signal.

For complex scenes and/or low bit rates, a number of visual artifacts may appear as a result of signal distortion from a compression system. The primary visual artifacts affecting current image compression systems are blocking effects and intermittent distortions, often near object boundaries, often called mosquito noise.
 15 Other artifacts include ripple, contouring, and loss of resolution.

Blocking effects generally result from discontinuities in the reconstructed signal's characteristics across block boundaries for a block-based coding system, *e.g.*, block DCT. Blocking effects are produced because adjacent blocks in an image are processed independently and the resulting independent distortion from block to block
 20 causes a lack of continuity between neighboring blocks. The lack of continuity may be in the form of abrupt changes in the signal intensity or signal gradient. In addition, block-type contouring, which is a special case of blocking effect, often results in instances when the intensity of an image is slowly changing.

Mosquito noise is typically seen when there is a sharp edge, *e.g.* an edge
 25 within a block separating two uniform but distinct regions. Block DCT applications are not effective at representing sharp edges. Accordingly, there is considerable distortion at sharp edges: the reconstructed edges are not as sharp as normal and the adjacent regions are not as uniform as they should be. Mosquito noise is especially evident in images containing text or computer graphics.

30 Many of the image compression standards available today, *e.g.* H.261, JPEG, MPEG-1; MPEG-2, and High Definition Television (HDTV), are based on block DCT

coding. Thus, most reproduced images may be adversely affected by blocking effects and edge distortion.

In addition to the image artifacts introduced by video signal compression and decompression, today's community antenna television (CATV), digital broadcast
5 satellite (DBS), and digital television (DTV) broadcasters, as well as, other deliverers of compressed digital images, are faced with a plethora of end user consumer electronics solutions for displaying the images. For example, consumer electronics manufacturers are presently offering HDTV, DTV, and analog TV units. Also on the
10 market are a wide range of personal computer (PC) based TV tuner cards that are capable of displaying full HDTV resolutions on appropriate multi-scan monitors. Indeed, multi-scan monitors with TV tuners are being made even larger to accommodate progressive scan signals on monitors that look like traditional TVs.

Digital TVs generally fall into three main categories: integrated high definition sets that include a digital receiver and display; digital set-top boxes designed to work
15 with HD and standard definition (SD) digital displays (and, in some cases, with current analog sets); and DTV-capable displays that, with the addition of a digital set-top box, offer a complete DTV system.

Heretofore, DTV receivers designated for the home theater market generally include a large-screen "digital ready" display and --at extra cost-- a separate set-top
20 box that encodes analog TV signals and provides the signals to the DTV receiver. As a result, consumers can watch big, beautiful, analog generated pictures now, and later, when more digital programming becomes available, they can purchase a decoder box to view digitally generated programming at HDTV resolutions.

These decoder boxes will also prolong the life of current analog TVs, as
25 consumers will be able to view digitally generated programming on their old TV set (*i.e.*, an analog black and white and/or color TV). Whether the set-top box is functioning as a encoder or a decoder both analog TVs and DTVs are adversely affected by the block DCT coding introduced image artifacts.

30 **SUMMARY OF THE INVENTION**

In response to these and other shortcomings of the prior art, the present

invention relates to a system and method for post-processing a bit stream comprising a decompressed representation of a compressed image or video. Briefly described, in architecture, the system can be implemented with a memory device, an image region segmenter, an artifact detector, and a filter. The region segmenter may be configured to sub-divide an image frame into a plurality of regions comprising a plurality of picture elements. Each region may be processed by the artifact detector to identify if a discontinuity between adjacent picture element data values is present in the region. Those regions identified as having a picture element data discontinuity may be forwarded to the filter to smooth the harshness of the picture element discontinuity.

10 The present invention can also be viewed as providing a method for reducing image artifacts in a compressed and decompressed image. In this regard, the method can be broadly summarized by the following steps: receiving picture element data associated with an image frame; segmenting the image frame into a plurality of regions; identifying regions within the image frame that include a possible image artifact; processing the identified regions with a filter such that at least one picture element data parameter is adjusted; and inserting the updated picture elements into the image frame.

BRIEF DESCRIPTION OF THE DRAWINGS

20 The invention can be better understood with reference to the following drawings. The components in the drawings are not necessarily to scale, emphasis instead being placed upon clearly illustrating the principles of the present invention. Moreover, in the drawings, like reference numerals designate corresponding parts throughout the several views.

25 FIG. 1 is a schematic diagram illustrating a possible operational environment for an image enhancing system.

FIG. 2 is a functional block diagram of the image enhancer of FIG. 1.

FIGs. 3A and 3B are schematic diagrams illustrating the operation of a region segmenter that may be associated with the image enhancer of FIG. 2.

30 FIG. 4 is a functional block diagram of an artifact detector that may be

associated with the region segmenter introduced in FIG. 2.

FIG. 5 is a functional block diagram of an adaptive filter that may be associated with the artifact detector of FIG. 4.

FIG. 6 is a flowchart illustrating a method for reducing image artifacts from an image frame that may be performed by the image enhancer of FIG. 2.

FIG. 7 is a flowchart illustrating a method for detecting image artifacts in a regional area as introduced in the flowchart of FIG. 6.

FIGs. 8A and 8B introduce portions of a flowchart illustrating a selective method for adjusting picture element data values as introduced in the flowchart of FIG. 6.

DETAILED DESCRIPTION OF A PREFERRED EMBODIMENT

Having summarized various aspects of the present invention, reference will now be made in detail to the description of the invention as illustrated in the drawings. While the invention will be described in connection with these drawings, there is no intent to limit it to the embodiment or embodiments disclosed therein. On the contrary, the intent is to cover all alternatives, modifications and equivalents included within the spirit and scope of the invention as defined by the appended claims.

Turning now to the drawings, wherein like referenced numerals designate corresponding parts throughout the drawings, reference is made to FIG. 1, which illustrates a schematic of an exemplary operational environment suited for an image enhancer. In this regard, an exemplary operational environment 10 may comprise a community antenna television (CATV) decoder 12, an image enhancer 100, a television receiver / monitor 14, and a multiple-unit remote control 20. As illustrated in FIG. 1, a coaxial cable 2 coupled to the CATV network may supply a broadband input signal comprising hundreds of digitally encoded and block discrete cosine transform (DCT) compressed video input signals to the CATV decoder 12. The compressed video signals may be compressed using the MPEG-2 video signal compression standard, other block DCT compression schemes, as well as, other digital processing methods. As shown in FIG. 1, the CATV decoder 12 may be coupled to the image enhancer 100 via a first coaxial cable 4. Similarly, the image enhancer 100

may be further coupled to the television receiver / monitor 14 via a second coaxial cable 6.

As also illustrated in FIG. 1, each of the CATV decoder 12, the image enhancer 100, and the television receiver / monitor 14 may be configured with a communications port 15, 105, and 17, respectively. As is well known, the communications ports 15, 105, and 17 may be configured to receive one or more remotely generated control signals 22, 24, 26 from one or more compatibly configured remote control devices 20. It will be appreciated that the remotely generated control signals 22, 24, and 26 may comprise radio frequency, infrared frequency, or other portions of the frequency spectrum. As is known, the remotely generated control signals 22, 24, and 26 may comprise on/off, input channel selection, mode selection, volume adjustment and other similar commands. In the specific case of the image enhancer 100, it is contemplated that the communication port 105 associated with the enhancer 100 may be configured to receive at least on/off, input channel selection, bypass mode selection, image artifact detection threshold, comparative adjustment threshold, region sensitivity, and block sensitivity commands from a remote control device 20.

Generally, the CATV decoder 12 will be configured to selectively demultiplex one or more compressed video signals and supply the demultiplexed signals to the input of an appropriately configured image decoder (not shown). For example, if the desired video signal is encoded with a MPEG-2 encoder, the image decoder (not shown) will be a MPEG-2 decoder. It will be appreciated that the nature of the video signal path previously described may vary greatly depending on the specific design of the television receiver / monitor 14 and any other desired video signal producing devices that may be added to the operational environment 10.

In a first example, the television receiver / monitor 14 may comprise an analog television (ATV). The ATV may provide composite, S-video, and component input jacks suited for receiving like analog video input signals from a number of devices, such as but not limited to, an analog video cassette recorder (VCR) (not shown), a video game console (not shown), a digital video disk (DVD) player (not shown), and the CATV decoder 12. In a second example, the television receiver / monitor 14 may

comprise a digital television (DTV). The DTV may provide a number of digital input jacks suited for receiving digital video input signals from a number of devices, such as but not limited to, a personal computer, a digital video disk (DVD) player with digital output capability (not shown), and the CATV decoder 12 (assuming the unit is
5 supplied with a digital video output jack). In a third example, the television receiver / monitor 14 may provide both analog input jacks as well as digital input jacks.

Regardless of the configuration of the television receiver / monitor 14, in those cases where the video compression scheme used to distribute the video signal used a block DCT technique, the video input signal at the television receiver / monitor 14
10 may be adversely affected by image artifacts as previously described. An image enhancer 100 in accordance with the present invention may be applied within the video signal path described with regard to FIG. 1 to reduce the harshness of edge discontinuities within an image region without removing high-frequency changes in image content from the image frame. It will be appreciated that the image enhancer
15 100 need not be a standalone device and may be integrated either within video devices designed to interface with the television receiver / monitor 14 (e.g., the CATV decoder 12) or alternatively within the television receiver / monitor analog receive signal path.

Reference is now directed to FIG. 2, which illustrates a functional block
20 diagram of the image enhancer 100 of FIG. 1. In this regard, the image enhancer 100 may be configured to receive a decompressed audio input signal 115 and a decompressed component video input signal 125 as well as a plurality of control signals 24 via the communications port 105. In response to these and possibly other inputs, the image enhancer 100 may provide an enhanced image output signal 155 as well as a
25 synchronized audio output signal 145.

As illustrated in FIG. 2, the image enhancer 100 may include a controller 110. The controller 110 may be configured to receive a plurality of input commands from the communications port 105 and in response to the commands may coordinate processing of the decompressed component video input signal 125. In addition, the controller 110
30 may be configured to monitor the real-time progress of the video image processing and may provide one or more control signals suited to synchronize the decompressed audio

input signal 115 with the enhanced image output signal 155. It will be appreciated by those skilled in the art, the controller 110 may comprise one or more application-specific integrated circuits (ASICs), a plurality of suitably configured logic gates, and other well known electrical configurations comprised of discrete elements both
5 individually and in various combinations to coordinate the overall operation of the image enhancer 100.

Furthermore, the image enhancer 100 may be implemented with a microprocessor and one or more memory devices, as well as other hardware and software components for coordinating the overall operation of the various elements
10 suited to enhance image signal information that may be supplied to the television receiver / monitor 14. In addition, it will be appreciated that the image enhancer 100 may include software, which comprises an ordered listing of executable instructions for implementing logical functions, which can be embodied in any computer-readable medium for use by or in connection with an instruction execution system, apparatus,
15 or device, such as a computer-based system, processor-containing system, or other system that can fetch the instructions from the instruction execution system, apparatus, or device and execute the instructions. The computer readable medium can be, for instance, an electronic, magnetic, optical, electromagnetic, infrared, or semiconductor system, apparatus, device, or propagation medium.

As illustrated in FIG. 2, the image enhancer 100 may provide a video bypass signal path that may include an input memory 130 communicatively coupled with an output memory 150. As shown in the block diagram of FIG. 2, the video bypass signal path receives the decompressed component video input signal 125 at an input port associated with the input memory device 130. The input memory device 130 may
25 comprise a frame memory suited to receive and process picture element information that may be used to generate an image. An input memory output signal 135 may be indirectly coupled to the enhanced image output signal 155 to complete the video bypass signal path. It should be appreciated that the video signal bypass path may be selected by an appropriately configured control signal 24 interpreted by the controller 110 and
30 resulting in a response, which disables devices in a video- processing path.

The video-processing path as illustrated in FIG. 2 may be inserted between the

input memory device 130 and the output memory 150 and may comprise a region segmenter 300, an artifact detector 400, and an adaptive filter 500. Each of the region segmenter 300, artifact detector 400, and adaptive filter 500 devices may be coupled in series with the region segmenter 300 receiving image information from the input memory 130 via the input memory output signal 135. In turn, the region segmenter supplies a portion of the frame to the artifact detector via a region segmenter output signal 305. Next, the artifact detector 400 supplies the adaptive filter 500 with image information associated with regions that contain a picture element data discontinuity via an artifact detector output signal 405. Last, the adaptive filter 500 supplies the output memory 150 with updated picture element data values via an adaptive filter output signal 505.

Operationally, the video-processing path of the image enhancer 100 may function as follows. The input memory 130 may receive image information from the decompressed video signal 125. In accordance with one or more control inputs from the controller 110, the input memory 130 may provide the image information to the region segmenter 300 via the input memory output signal 135. The region segmenter 300 may format the information by subdividing the information into a plurality of $M \times M$ picture element regions in response to a region sensitivity value, M , that may be supplied or derived via a command generated by the remote control 20 (FIG. 1). The region sensitivity value, M , may then be forwarded to the controller 110 via the communications port 105 for further distribution as necessary throughout the various elements of the image enhancer 100. It will be appreciated that the region segmenter 300 may start by defining an image frame reference picture element and may sub-divide the image frame into a plurality of $M \times M$ regions by systematically advancing every M picture elements in a horizontal or vertical direction across the picture elements to designate a reference picture element for the next $M \times M$ region. After a row or column of picture elements is exhausted, the region segmenter 300 may be configured to advance M picture elements vertically or horizontally, respectively, depending upon which direction is selected as the first direction to advance through the picture element array. It should be further appreciated that it may be preferable to select values of M such that M is a factor of the both the number of picture elements in the horizontal and

the number of picture elements in the vertical direction in the image frame to be processed. In this way, each of the $M \times M$ regions will contain the same number of picture elements.

After having segmented the image frame into a plurality of $M \times M$ region
 5 segments, the region segmenter 300 may provide the artifact detector 400 with a reference indicator for each of the plurality of a regions along with the individual picture element information associated with the picture elements contained within each respective region via the region segmenter output signal 305.

In turn, the artifact detector 400 may be configured to receive each $M \times M$
 10 regional array of picture elements and perform one or more statistical tests on at least one picture element data element associated with each of the picture elements in the region of interest. The artifact detector 400 may be further configured to compare the results of the one or more statistical tests with an image artifact detection threshold, DET_{TH} , which may be supplied by the controller 110 to determine if the region of
 15 interest is likely to contain an image artifact. When one or more of the statistical tests result in a value that exceeds the image artifact detection threshold, DET_{TH} , the artifact detector 400 may be configured to forward the region along with an identifier suited to locate the region within the image frame to the adaptive filter 500 via the artifact detector output signal 405.

20 Next the adaptive filter 500 may be configured to receive original picture element information from the entire frame from the input memory 130 along with the identified regions with image artifacts and the image information associated with the artifact affected regions. In addition, the adaptive filter 500 may receive a block sensitivity value, N , and a comparative adjustment threshold, $COMP_{TH}$. It is
 25 significant to note that the block sensitivity value, N , may or may not be associated with the size of the block of picture elements used by the standard video compression technique to compress/decompress the video signal prior to introduction to the image enhancer 100. The only limitation on the magnitude of the block sensitivity value, N , is that it is smaller in magnitude than the region sensitivity value, M .

30 As will be explained in greater detail with regard to the discussion of FIGs. 5, 6, and 8A and 8B, the adaptive filter 500 may be configured to progressively compare at

least one picture element data value associated with each of the picture elements comprising each of the identified regions affected by an image artifact with each of its nearest neighbors in a first comparative scan direction. If the comparison result for a particular picture element comparison exceeds the comparative adjustment threshold, $COMP_{TH}$, and the picture element comparison coincides with a $N \times N$ block boundary within the region of interest, the present picture element data value is adjusted. Otherwise, if the picture element comparison is performed between picture elements within a $N \times N$ block the present picture element under test is not adjusted. In this way, image artifacts that result from the loss of data information in the image compression/decompression may be filtered or smoothed without removing high-frequency picture element data transitions that were present in the original image.

As illustrated in FIG. 2, the image enhancer 100 may use the output memory device 150 to assemble an enhanced image frame output 155 that may be forwarded to the television receiver / monitor 14 (FIG. 1). In this regard, the output memory device 150 may be configured to receive the input memory output signal 135 as well as any adjusted picture elements from the adaptive filter 500 via the adaptive filter output signal 505. The output memory 150 may be configured to simply replace original picture element information associated with respective picture elements that have been adjusted by the adaptive filter 500.

Reference is now directed to FIG. 3A, which illustrates an example of an image region. In this regard, FIG. 3A illustrates a single example of an 8×8 region 310. As illustrated, the region 310 may be defined by a region reference 320, which may comprise one of the corner picture elements of the region 310. It will be appreciated that a corner picture element is preferred to identify the region 310 in order to simplify individual picture element data transfers and calculations. As shown, individual picture elements may be identified by their relative position from the region reference 320 by using a horizontal counter, i , and a vertical counter, j . Using this picture element identification scheme, an exemplary picture element 322 may be otherwise known as $P_{5,3}$. Each of the 63 remaining picture elements may be similarly indexed. It should be appreciated that separate and distinct regions 310 will continue in a two-dimensional array such as to form the complete image frame.

Reference is now directed to FIG. 3B, which presents a second example of an 8x8 region 310, as well as, two fundamental concepts associated with the image enhancer 100 (FIGs. 1 and 2). As illustrated in FIG. 3B, a portion of the region 310 may be further subdivided by a plurality of $N \times N$ image blocks 330 (two 3x3 blocks shown for example only). As will be further explained in association with the adaptive filter 500 and the method for reducing image artifacts in a discrete cosine transform (DCT) compressed and decompressed image, the image blocks 330 serve to identify image sub-regions that should comprise fairly accurate image information as a result of the nature of block DCT based data compression/decompression techniques. It is expected that image artifacts are most often introduced at the edges of the sub-regions or image blocks 330. As a result, it is contemplated that picture elements that share an edge with an image block 330 may be suitable for adjustment by the image enhancer 100.

It should be appreciated that in practice it may be advantageous to set the block sensitivity value, N , such that it is equivalent with the block size used in the original block DCT compression/decompression technique used to generate the image frame. However, it is contemplated that for certain viewers and certain types of image content, it may be advantageous to select other block sensitivity values, N , as may suit the individual viewing tastes of the viewer.

In addition to the concept of using block edges to selectively identify picture elements suited for adjustment, FIG. 3B illustrates a second fundamental concept associated with the image enhancer 100 (FIGs. 1 and 2). In this regard, attention is directed to picture element 322 (*i.e.*, $P_{5,3}$). As shown in FIG. 3B, it is contemplated that an image smoothing comparison be performed for at least one picture element data value associated with each picture element within the region 310 and at least one of the picture element's 322 nearest neighbors.

It will be appreciated by those skilled in the art that in order to construct an operationally efficient adaptive filter 500 a determination may be made as to whether a picture element of interest resides at an intersection between adjacent blocks 330. If the result of the determination is affirmative, the adaptive filter may proceed to compare and adjust one or more data values associated with the picture element of interest. In this

way, the processing time associated with picture elements within the interior of an image block 330 can be avoided.

The relationships between an image region 310, image blocks 330, and picture elements 322 having been briefly described with regard to FIGs. 3A and 3B, reference is now directed to FIG. 4, which presents a functional block diagram of the artifact detector 400 introduced in the image enhancer 100 FIG. 2. In this regard, the artifact detector may include a mean value calculator 410, a maximum value detector 420, a minimum value detector 430, and a region discontinuity identifier 440. As illustrated in FIG. 4, the region segmenter output signal 305 may be supplied to each of the mean value calculator 410, maximum (max.) value detector 420, and the minimum (min.) value detector 430. In turn, each of the devices may generate a result indicative of one or more picture element data values associated with the picture elements 322 (FIGs. 3A and 3B) that comprise the region 310. As illustrated in FIG. 4, a mean value calculator output, a max. value detector output, and a min. value detector output may be forwarded to the region discontinuity identifier 440.

The region discontinuity identifier 440 may be communicatively coupled with the controller 110 (FIG. 2) to receive the image artifact detection threshold, DET_{TH} . The region discontinuity identifier 440 may be configured to generate the absolute value of the difference between both the min. and the max. picture element data values within the region with the mean picture element data value for the region. In addition, the region discontinuity identifier 440 may be configured to compare the differences with the image artifact detection threshold supplied by the controller 110 (FIG. 2). For those image regions where either of the differences exceeds the artifact detection threshold, the region discontinuity identifier may be configured to forward an identifier for the region 310 as well as the picture element information associated with the individual picture elements contained within the region to the artifact detector output signal 445.

Reference is now directed to FIG. 5, which presents a functional block diagram of an adaptive filter that may be associated with the artifact detector of FIG. 4. In this regard, the adaptive filter 500 may include a filter controller 510, a buffer 520, a selective picture element adjuster 530, and a region memory 540. As illustrated in

FIG. 5, the adaptive filter 500 may be configured to receive the artifact detector output signal 445 as well as a plurality of inputs from the controller 110 (FIG. 2). After possibly selectively adjusting one or more data values associated with the individual picture elements of the present region 310 (see FIGs. 3A and 3B), the adaptive filter
 5 may be configured to provide an adjusted image data output signal 505.

Operationally, the adaptive filter 500 may store an identifier along with the picture element data associated with a region previously identified in the artifact detector 400 as having an image artifact in the buffer 520. The filter controller 510 may be configured to receive the picture element comparison threshold and the block
 10 sensitivity value from the controller 110 (FIG. 2). The filter controller 510 may be configured to provide these values to the selective picture element adjuster 530. As illustrated in the functional block diagram of FIG. 5, the selective picture element adjuster 530 may receive a region of data from the buffer 520. Having received the controller 110 input values and a region of picture element data values, the selective
 15 picture element adjuster 530 may proceed to perform an element by element comparison of at least one picture element data value associated with each picture element and those of its nearest neighbors. It should be appreciated that the comparison may include only picture elements in a select relationship (e.g., horizontal and adjacent, vertical and adjacent, or diagonal and adjacent) with one another. It
 20 should be further appreciated that the comparison may include a mathematical combination between a picture element of interest and its nine adjacent picture elements. Regardless of the comparison performed, it is contemplated that the selective picture element adjuster modify only picture elements that form an intersection between adjacent blocks as identified by the block sensitivity value and
 25 where the picture element comparison exceeds the picture element comparison threshold. The picture element modification may comprise a mathematical combination of a picture element of interest and one or more adjacent picture elements.

As further illustrated in FIG. 5, modified picture element values may be
 30 forwarded to the region memory 540 where the values may be temporarily buffered. After having systematically analyzed the picture element data values for the region by

proceeding in a first direction, (e.g., horizontally or vertically) the selective picture element adjuster 530 may be configured to analyze the data in a second direction different from the first direction using the original picture element data values for picture elements not adjusted in the first analysis along with updated (*i.e.*, buffered) values for picture elements modified during the first analysis. After having smoothed image artifacts from the region, the adaptive filter 500 may be configured to forward the contents of the region memory 540 via the adaptive filter output 505 to the output memory 150 (FIG. 2). The output memory 150 may be configured to receive each of the smoothed regions from the adaptive filter 500 and generate an image artifact reduced image frame by replacing only the smoothed regions in the image frame.

In an alternative embodiment, the adaptive filter 500 may be replaced by an edge-preserving low-pass filter (not shown). The edge-preserving low-pass filter may be applied to reduce contouring artifacts frequently visible in image areas with little high-frequency content, such as in a background or border that appears to have a solid color. As previously described, while image areas may appear to comprise a single solid color, various image compression and decompression techniques in combination with post decompression processors may introduce image artifacts visible within the affected image areas. An edge-preserving low-pass filter may be configured to retain detail associated with a boundary or edge, while smoothing or reducing the harshness between image artifact affected pixels.

The various elements of an image enhancer 100 having been introduced and described with regard to FIGs. 2 through 5, reference is now directed to FIG. 6, which illustrates a method for reducing image artifacts from an image frame that may be performed by the image enhancer 100 of FIG. 2. In this regard, a method for reducing image artifacts 600 may begin with step 602, herein labeled, "Start." Next, in a system initialization step, the method for reducing image artifacts 600 may set an artifact detection threshold, a region sensitivity, a block sensitivity, and a picture element data value comparison threshold as shown in step 604. A video-processing loop may begin with step 606 where the method for reducing image artifacts 600 receives a decoded image frame. Next, in step 608, the method for reducing image artifacts 600 may perform a regional artifact detection process by analyzing picture

element data values in a $M \times M$ region. As previously described with regard to FIG. 4, an artifact detector 400 may be designed to identify a plurality of sub-regions of a larger image frame that may include an image artifact by performing one or more statistical tests on the picture element data values associated with the picture elements within the region.

Once regions of the image frame that may contain an image artifact have been identified in step 608, the method for reducing image artifacts 600 may proceed to store both an identifier for each of the regions along with the associated picture element data values for each of the regions with an image artifact as illustrated in step 610. Next, the method for reducing image artifacts 600 may perform a pixel adjustment process as shown in step 612. As previously described with regard to FIG. 5, an adaptive filter 500 may be configured to smooth image artifacts by selectively adjusting one or more picture element data values associated with picture elements that define a block transition. The adjustment may take the form of a mathematical combination of one or more picture element data values associated with adjacent picture elements of a particular picture element of interest.

For example, the mean luminance of the eight adjacent picture elements may be determined and weighted before performing a second mean calculation between the original picture element luminance value and the interim result. In another example, the luminance value of a particular picture element of interest may be combined with the luminance value associated with its horizontally or vertically adjacent nearest neighbors, with the mean luminance value of the original picture element data values replacing the original data value for the picture element of interest. It will be appreciated that color information associated with individual picture element may be analyzed as well by these and other arrangements of neighboring picture elements.

After having completed the picture element analysis and adjustment process in step 612, the method for reducing image artifacts 600 may proceed to buffer the modified picture elements as illustrated in step 614. Next, the method for reducing image artifacts 600 may insert the modified and buffered picture elements into the appropriate locations within the image frame as indicated in step 616. As further illustrated by the flow control arrow of the flowchart of FIG. 6, steps 606 through 616

may be repeated as required to process each successive image frame that together form a video. After detecting an appropriate input indicative of a loss of frame data, a user selected "off" mode request, or the like, the method for reducing image artifacts 600 may terminate as indicated in step 618, herein labeled, "Stop."

5 The method for reducing image artifacts 600 having been introduced and briefly described with regard to the flowchart of FIG. 6, reference is now directed to FIG. 7, which illustrates a method for detecting image artifacts in a regional area as may be performed in step 608 shown in the flowchart of FIG. 6. In this regard, a method for detecting image artifacts 608 may begin with step 700, herein labeled,
10 "Start." In step 702, the method for detecting image artifacts 608 may retrieve a regional sensitivity value, M , and an image artifact detection threshold, DET_{TH} . Next, in step 704, the method for detecting image artifacts 608 may identify a present region of interest defined by the regional sensitivity value, M . In step 706, the method for detecting image artifacts 608 may calculate a picture element data value mean for the
15 region, as well as, identify the picture element data value extrema value(s) for the region such as, for example, a picture element data value minimum value and/or a picture element data value maximum value for the region.

 The method for detecting image artifacts 608 may then check whether the absolute value of the difference between the picture element data value minimum
20 value for the region and the mean value for the region exceeds the magnitude of the image artifact detection threshold as indicated in the query of step 708. If the determination in step 706 is affirmative, the method for detecting image artifacts 608 may perform step 710 where the region identifier and the associated picture element data values for the region may be buffered. Otherwise, if the determination in step
25 706 is negative, the method for detecting image artifacts may proceed to step 712.

 Similarly, the method for detecting image artifacts 608 may then check whether the absolute value of the difference between the picture element data value maximum for the region and the mean value for the region exceeds the magnitude of
30 the image artifact detection threshold as indicated in the query of step 712. If the determination in step 712 is affirmative, the method for detecting image artifacts 608 may perform step 714 where the region identifier and the associated picture element

data values for the region may be buffered. Otherwise, if the result of the query in step 712 is negative, the method for detecting image artifacts 608 may be configured to perform step 716 where as illustrated the region identifier may be incremented.

The method for detecting image artifacts 608 may proceed by determining if
 5 all regions have been analyzed as illustrated in the query of step 718. If the determination in step 718 is negative, the method for detecting image artifacts 608 may return to repeat steps 706 through 718 as required to analyze the image frame. Otherwise, if the determination in step 718 is affirmative, *i.e.*, all image regions have been analyzed, the method for detecting image artifacts 608 may be terminated as
 10 indicated in step 720, herein labeled, "Stop."

The method for detecting image artifacts 608 having been described with regard to the flowchart of FIG. 7, reference is now directed to FIGs. 8A and 8B, which illustrate a method for selectively adjusting picture element data values as referenced in step 612 of the flowchart of FIG. 6. In this regard, a method for selectively
 15 adjusting picture element data values 612 may begin with step 800, herein labeled, "Start." In step 802, the method for selectively adjusting picture element data values 612 may retrieve a smoothing threshold, $COMP_{TH}$, and a desired first analysis direction. Next, in step 804, the method for selectively adjusting picture element data values 612 may retrieve picture element data values associated with each of the
 20 picture elements contained within a region previously identified as containing an image artifact. In step 806, the method for selectively adjusting picture element data values 612 may initialize directional counters and maximum values associated with the size of the region.

The method for selectively adjusting picture element data values 612 may
 25 perform a mathematical combination in step 808 in order to compare a present picture element of interest with its nearest neighbor in a first direction as defined by the counters in step 806. In step 810, the result of the mathematical combination performed in step 808 may be compared with the smoothing threshold. If the query of step 810 indicates that the result in step 808 exceeds the smoothing threshold, the
 30 method for selectively adjusting picture element data values 612 may be configured to perform a second query as illustrated in step 812 to determine if the picture elements

compared in step 808 form a boundary that coincides with a block boundary. If the result of the query in step 812 is affirmative, the present picture element may be adjusted as indicated in step 814. It will be appreciated that this adjustment may take the form of an averaging, including a weighted average of the present picture element and its nearest neighbors within the region as long as the condition holds true that the compared picture elements (see step 808) do not form a block boundary.

As illustrated in the flowchart of FIG. 8A, if either the query of step 810 or the query of step 812 result in a negative result, or step 814 has been performed, the method for selectively adjusting picture element data values 612 may continue by incrementing the first directional counter as illustrated in step 816.

Reference is now directed to FIG. 8B, which presents a continuation of the method for selectively adjusting picture element data values 612. In this regard, the method for selectively adjusting picture element data values 612 may continue after connector "A" by making a determination if all picture elements in the first direction have been processed as illustrated in step 818. If the result of the query in step 818 is affirmative, the method for selectively adjusting picture element data values 612 may perform another query to determine if all picture elements in the region have been processed as shown in step 822. If the result of the query in step 822 is affirmative, the method for selectively adjusting picture element data values 612 may increment a region counter and return via connector "C" to step 804 (FIG. 8A) and steps 804 through 824 may be repeated as necessary. Otherwise, if the result of the query in step 822 is negative, the method for selectively adjusting picture element data values 612 may perform a check to see if all image regions with artifacts have been processed as indicated in the query of step 826. If the result of the query in step 826 is negative, the method for selectively adjusting picture element data values 612 may return via connector "B" to step 808 (FIG. 8A) and steps 808 through 826 may be repeated as necessary. Otherwise, if the result of the query in step 826 is affirmative (i.e., all identified image regions have been smoothed) the method for selectively adjusting picture element data values 612 may terminate as indicated in step 828.

Any process descriptions or blocks in flow charts of FIGs. 6, 7, and 8A-8B, should be understood as representing modules, segments, or portions of code which

include one or more executable instructions for implementing specific logical functions or steps in the associated process. Alternate implementations are included within the scope of the present invention in which functions may be executed out of order from that shown or discussed, including substantially concurrently or in reverse order, depending on the functionality involved, as would be understood by those reasonably skilled in the art of the present invention.

While the image enhancer 100 may be implemented in one or more hardware based configurations so as to provide the necessary processing speed to smooth video image frames at a reasonable frame rate, it will be appreciated that an image enhancer 100 in accordance with the teachings and concepts of the present invention may be implemented in software operable on a computing device such as but not limited to a special or general purpose digital computer, such as a personal computer (PC; IBM-compatible, Apple-compatible, or otherwise), workstation, minicomputer, or mainframe computer.

When the image enhancer 100 is implemented in software, it should be noted that the processing step as previously described in association with the flowcharts of FIGs. 6, 7, and 8A-8B can be stored on any computer readable medium for use by or in connection with any computer related system or method.

In the context of this document, a computer readable medium is an electronic, magnetic, optical, or other physical device or means that can contain or store a computer program for use by or in connection with a computer related system or method. The image enhancer 100 can be embodied in any computer-readable medium for use by or in connection with an instruction execution system, apparatus, or device, such as a computer-based system, processor-containing system, or other system that can fetch the instructions from the instruction execution system, apparatus, or device and execute the instructions. The computer readable medium can be, for example but not limited to, an electronic, magnetic, optical, electromagnetic, infrared, or semiconductor system, apparatus, device, or propagation medium. More specific examples (a non-exhaustive list) of the computer-readable medium would include the following: an electrical connection (electronic) having one or more wires, a portable computer diskette (magnetic), a random access memory (RAM) (electronic), a read-

only memory (ROM) (electronic), an erasable programmable read-only memory (EPROM, EEPROM, or Flash memory) (electronic), an optical fiber (optical), and a portable compact disc read-only memory (CDROM) (optical). Note that the computer-readable medium could even be paper or another suitable medium upon

5 which the program is printed, as the program can be electronically captured, via for instance optical scanning of the paper or other medium, then compiled, interpreted or otherwise processed in a suitable manner if necessary, and then stored in a computer memory.

10

11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
61
62
63
64
65
66
67
68
69
70
71
72
73
74
75
76
77
78
79
80
81
82
83
84
85
86
87
88
89
90
91
92
93
94
95
96
97
98
99
100
101
102
103
104
105
106
107
108
109
110
111
112
113
114
115
116
117
118
119
120
121
122
123
124
125
126
127
128
129
130
131
132
133
134
135
136
137
138
139
140
141
142
143
144
145
146
147
148
149
150
151
152
153
154
155
156
157
158
159
160
161
162
163
164
165
166
167
168
169
170
171
172
173
174
175
176
177
178
179
180
181
182
183
184
185
186
187
188
189
190
191
192
193
194
195
196
197
198
199
200
201
202
203
204
205
206
207
208
209
210
211
212
213
214
215
216
217
218
219
220
221
222
223
224
225
226
227
228
229
230
231
232
233
234
235
236
237
238
239
240
241
242
243
244
245
246
247
248
249
250
251
252
253
254
255
256
257
258
259
260
261
262
263
264
265
266
267
268
269
270
271
272
273
274
275
276
277
278
279
280
281
282
283
284
285
286
287
288
289
290
291
292
293
294
295
296
297
298
299
300
301
302
303
304
305
306
307
308
309
310
311
312
313
314
315
316
317
318
319
320
321
322
323
324
325
326
327
328
329
330
331
332
333
334
335
336
337
338
339
340
341
342
343
344
345
346
347
348
349
350
351
352
353
354
355
356
357
358
359
360
361
362
363
364
365
366
367
368
369
370
371
372
373
374
375
376
377
378
379
380
381
382
383
384
385
386
387
388
389
390
391
392
393
394
395
396
397
398
399
400
401
402
403
404
405
406
407
408
409
410
411
412
413
414
415
416
417
418
419
420
421
422
423
424
425
426
427
428
429
430
431
432
433
434
435
436
437
438
439
440
441
442
443
444
445
446
447
448
449
450
451
452
453
454
455
456
457
458
459
460
461
462
463
464
465
466
467
468
469
470
471
472
473
474
475
476
477
478
479
480
481
482
483
484
485
486
487
488
489
490
491
492
493
494
495
496
497
498
499
500
501
502
503
504
505
506
507
508
509
510
511
512
513
514
515
516
517
518
519
520
521
522
523
524
525
526
527
528
529
530
531
532
533
534
535
536
537
538
539
540
541
542
543
544
545
546
547
548
549
550
551
552
553
554
555
556
557
558
559
560
561
562
563
564
565
566
567
568
569
570
571
572
573
574
575
576
577
578
579
580
581
582
583
584
585
586
587
588
589
590
591
592
593
594
595
596
597
598
599
600
601
602
603
604
605
606
607
608
609
610
611
612
613
614
615
616
617
618
619
620
621
622
623
624
625
626
627
628
629
630
631
632
633
634
635
636
637
638
639
640
641
642
643
644
645
646
647
648
649
650
651
652
653
654
655
656
657
658
659
660
661
662
663
664
665
666
667
668
669
670
671
672
673
674
675
676
677
678
679
680
681
682
683
684
685
686
687
688
689
690
691
692
693
694
695
696
697
698
699
700
701
702
703
704
705
706
707
708
709
710
711
712
713
714
715
716
717
718
719
720
721
722
723
724
725
726
727
728
729
730
731
732
733
734
735
736
737
738
739
740
741
742
743
744
745
746
747
748
749
750
751
752
753
754
755
756
757
758
759
760
761
762
763
764
765
766
767
768
769
770
771
772
773
774
775
776
777
778
779
780
781
782
783
784
785
786
787
788
789
790
791
792
793
794
795
796
797
798
799
800
801
802
803
804
805
806
807
808
809
810
811
812
813
814
815
816
817
818
819
820
821
822
823
824
825
826
827
828
829
830
831
832
833
834
835
836
837
838
839
840
841
842
843
844
845
846
847
848
849
850
851
852
853
854
855
856
857
858
859
860
861
862
863
864
865
866
867
868
869
870
871
872
873
874
875
876
877
878
879
880
881
882
883
884
885
886
887
888
889
890
891
892
893
894
895
896
897
898
899
900
901
902
903
904
905
906
907
908
909
910
911
912
913
914
915
916
917
918
919
920
921
922
923
924
925
926
927
928
929
930
931
932
933
934
935
936
937
938
939
940
941
942
943
944
945
946
947
948
949
950
951
952
953
954
955
956
957
958
959
960
961
962
963
964
965
966
967
968
969
970
971
972
973
974
975
976
977
978
979
980
981
982
983
984
985
986
987
988
989
990
991
992
993
994
995
996
997
998
999
1000
1001
1002
1003
1004
1005
1006
1007
1008
1009
1010
1011
1012
1013
1014
1015
1016
1017
1018
1019
1020
1021
1022
1023
1024
1025
1026
1027
1028
1029
1030
1031
1032
1033
1034
1035
1036
1037
1038
1039
1040
1041
1042
1043
1044
1045
1046
1047
1048
1049
1050
1051
1052
1053
1054
1055
1056
1057
1058
1059
1060
1061
1062
1063
1064
1065
1066
1067
1068
1069
1070
1071
1072
1073
1074
1075
1076
1077
1078
1079
1080
1081
1082
1083
1084
1085
1086
1087
1088
1089
1090
1091
1092
1093
1094
1095
1096
1097
1098
1099
1100
1101
1102
1103
1104
1105
1106
1107
1108
1109
1110
1111
1112
1113
1114
1115
1116
1117
1118
1119
1120
1121
1122
1123
1124
1125
1126
1127
1128
1129
1130
1131
1132
1133
1134
1135
1136
1137
1138
1139
1140
1141
1142
1143
1144
1145
1146
1147
1148
1149
1150
1151
1152
1153
1154
1155
1156
1157
1158
1159
1160
1161
1162
1163
1164
1165
1166
1167
1168
1169
1170
1171
1172
1173
1174
1175
1176
1177
1178
1179
1180
1181
1182
1183
1184
1185
1186
1187
1188
1189
1190
1191
1192
1193
1194
1195
1196
1197
1198
1199
1200
1201
1202
1203
1204
1205
1206
1207
1208
1209
1210
1211
1212
1213
1214
1215
1216
1217
1218
1219
1220
1221
1222
1223
1224
1225
1226
1227
1228
1229
1230
1231
1232
1233
1234
1235
1236
1237
1238
1239
1240
1241
1242
1243
1244
1245
1246
1247
1248
1249
1250
1251
1252
1253
1254
1255
1256
1257
1258
1259
1260
1261
1262
1263
1264
1265
1266
1267
1268
1269
1270
1271
1272
1273
1274
1275
1276
1277
1278
1279
1280
1281
1282
1283
1284
1285
1286
1287
1288
1289
1290
1291
1292
1293
1294
1295
1296
1297
1298
1299
1300
1301
1302
1303
1304
1305
1306
1307
1308
1309
1310
1311
1312
1313
1314
1315
1316
1317
1318
1319
1320
1321
1322
1323
1324
1325
1326
1327
1328
1329
1330
1331
1332
1333
1334
1335
1336
1337
1338
1339
1340
1341
1342
1343
1344
1345
1346
1347
1348
1349
1350
1351
1352
1353
1354
1355
1356
1357
1358
1359
1360
1361
1362
1363
1364
1365
1366
1367
1368
1369
1370
1371
1372
1373
1374
1375
1376
1377
1378
1379
1380
1381
1382
1383
1384
1385
1386
1387
1388
1389
1390
1391
1392
1393
1394
1395
1396
1397
1398
1399
1400
1401
1402
1403
1404
1405
1406
1407
1408
1409
1410
1411
1412
1413
1414
1415
1416
1417
1418
1419
1420
1421
1422
1423
1424
1425
1426
1427
1428
1429
1430
1431
1432
1433
1434
1435
1436
1437
1438
1439
1440
1441
1442
1443
1444
1445
1446
1447
1448
1449
1450
1451
1452
1453
1454
1455
1456
1457
1458
1459
1460
1461
1462
1463
1464
1465
1466
1467
1468
1469
1470
1471
1472
1473
1474
1475
1476
1477
1478
1479
1480
1481
1482
1483
1484
1485
1486
1487
1488
1489
1490
1491
1492
1493
1494
1495
1496
1497
1498
1499
1500
1501
1502
1503
1504
1505
1506
1507
1508
1509
1510
1511
1512
1513
1514
1515
1516
1517
1518
1519
1520
1521
1522
1523
1524
1525
1526
1527
1528
1529
1530
1531
1532
1533
1534
1535
1536
1537
1538
1539
1540
1541
1542
1543
1544
1545
1546
1547
1548
1549
1550
1551
1552
1553
1554
1555
1556
1557
1558
1559
1560
1561
1562
1563
1564
1565
1566
1567
1568
1569
1570
1571
1572
1573
1574
1575
1576
1577
1578
1579
1580
1581
1582
1583
1584
1585
1586
1587
1588
1589
1590
1591
1592
1593
1594
1595
1596
1597
1598
1599
1600
1601
1602
1603
1604
1605
1606
1607
1608
1609
1610
1611
1612
1613
1614
1615
1616
1617
1618
1619
1620
1621
1622
1623
1624
1625
1626
1627
1628
1629
1630
1631
1632
1633
1634
1635
1636
1637
1638
1639
1640
1641
1642
1643
1644
1645
1646
1647
1648
1649
1650
1651
1652
1653
1654
1655
1656
1657
1658
1659
1660
1661
1662
1663
1664
1665
1666
1667
1668
1669
1670
1671
1672
1673
1674
1675
1676
1677
1678
1679
1680
1681
1682
1683
1684
1685
1686
1687
1688
1689
1690
1691
1692
1693
1694
1695
1696
1697
1698
1699
1700
1701
1702
1703
1704
1705
1706
1707
1708
1709
1710
1711
1712
1713
1714
1715
1716
1717
1718
1719
1720
1721
1722
1723
1724
1725
1726
1727
1728
1729
1730
1731
1732
1733
1734
1735
1736
1737
1738
1739
1740
1741
1742
1743
1744
1745
1746
1747
1748
1749
1750
1751
1752
1753
1754
1755
1756
1757
1758
1759
1760
1761
1762
1763
1764
1765
1766
1767
1768
1769
1770
1771
1772
1773
1774
1775
1776
1777
1778
1779
1780
1781
1782
1783
1784
1785
1786
1787
1788
1789
1790
1791
1792
1793
1794
1795
1796
1797
1798
1799
1800
1801
1802
1803
1804
1805
1806
1807
1808
1809
1810
1811
1812
1813
1814
1815
1816
1817
1818
1819
1820
1821
1822
1823
1824
1825
1826
1827
1828
1829
1830
1831
1832
1833
1834
1835
1836
1837
1838
1839
1840
1841
1842
1843
1844
1845
1846
1847
1848
1849
1850
1851
1852
1853
1854
1855
1856
1857
1858
1859
1860
1861
1862
1863
1864
1865
1866
1867
1868
1869
1870
1871
1872
1873
1874
1875
1876
1877
1878
1879
1880
1881
1882
1883
1884
1885
1886
1887
1888
1889
1890
1891
1892
1893
1894
1895
1896
1897
1898
1899
1900
1901
1902
1903
1904
1905
1906
1907
1908
1909
1910
1911
1912
1913
1914
1915
1916
1917
1918
1919
1920
1921
1922
1923
1924
1925
1926
1927
1928
1929
1930
1931
1932
1933
1934
1935
1936
1937
1938
1939
1940
1941
1942
1943
1944
1945
1946
1947
1948
1949
1950
1951
1952
1953
1954
1955
1956
1957
1958
1959
1960
1961
1962
1963
1964
1965
1966
1967
1968
1969
1970
1971
1972
1973
1974
1975
1976
1977
1978
1979
1980
1981
1982
1983
1984
1985
1986
1987
1988
1989
1990
1991
1992
1993
1994
1995
1996
1997
1998
1999
2000
2001
2002
2003
2004
2005
2006
2007
2008
2009
2010
2011
2012
2013
2014
2015
2016
2017
2018
2019
2020
2021
2022
2023
2024
2025
2026
2027
2028
2029
2030
2031
2032
2033
2034
2035
2036
2037
2038
2039
2040
2041
2042
2043
2044
2045
2046
2047
2048
2049
2050
2051
2052
2053
2054
2055
2056
2057
2058
2059
2060
2061
2062
2063
2064
2065
2066
2067
2068
2069
2070
2071
2072
2073
2074
2075
2076
2077
2078
2079
2080
2081
2082
2083
2084
2085
2086
2087
2088
2089
2090
2091
2092
2093
2094
2095
2096
2097
2098
2099
2100
2101
2102
2103
2104
2105
2106
2107
2108
2109
2110
2111
2112
2113
2114
2115
2116
2117
2118
2119
2120
2121
2122
2123
2124
2125
2126
2127
2128
2129
2130
2131
2132
2133
2134
2135
2136
2137
2138
2139
2140
2141
2142
2143
2144
2145
2146
2147
2148
2149
2150
2151
2152
2153
2154
2155
2156
2157
2158
2159
2160
2161
2162
2163
2164
2165
2166
2167
2168
2169
2170
2171
2172
2173
2174
2175
2176
2177
2178
2179
2180
2181
2182
2183
2184
2185
2186
2187
2188
2189
2190
2191
2192
2193
2194
2195
2196
2197
2198
2199
2200
2201
2202
2203
2204
2205
2206
2207
2208
2209
2210
2211
2